

**\*\*DRAFT02\*\* Search for the Decay  $K^+ \rightarrow \pi^+ \gamma \gamma$   
in the  $\pi^+$  Momentum Region  $P > 213 \text{ MeV}/c$**

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## Abstract

We have performed a search for the  $K^+ \rightarrow \pi^+ \gamma \gamma$  decay at rest in the kinematic region with  $\pi^+$  momentum close to the end point. No events were observed, and a 90% confidence-level upper limit on the partial branching ratio  $\mathcal{B}(K^+ \rightarrow \pi^+ \gamma \gamma, P > 213 \text{ MeV}/c)$  is determined to be  $8.3 \times 10^{-9}$  under the assumption of the chiral perturbation theory including next-to-leading order “unitarity” corrections. The same data were used to set an upper limit on the  $K^+ \rightarrow \pi^+ \gamma$  branching ratio to  $2.3 \times 10^{-9}$ . We also report improved limits on the rates of  $K^+ \rightarrow \pi^+ X^0$  and  $X^0 \rightarrow \gamma \gamma$ , where  $X^0$  is a hypothetical short-lived neutral particle.

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We report the results of a new search for the rare decay  $K^+ \rightarrow \pi^+ \gamma \gamma$  in the  $\pi^+$  momentum region  $P > 213$  MeV/ $c$  from the E949 experiment [1] at the Alternating Gradient Synchrotron (AGS) of Brookhaven National Laboratory (BNL). The first observation of the decay in the  $\pi^+$  momentum from 100 to 180 MeV/ $c$  was reported [2] by the BNL-E787 experiment with the corresponding partial branching ratio  $\mathcal{B}(K^+ \rightarrow \pi^+ \gamma \gamma, 100 \text{ MeV}/c < P < 180 \text{ MeV}/c)$  of  $[6.0 \pm 1.5(\text{stat}) \pm 0.7(\text{syst})] \times 10^{-7}$ . In the  $\pi^+$  momentum region greater than 215 MeV/ $c$ , no  $K^+ \rightarrow \pi^+ \gamma \gamma$  decay was observed.

In an effective-field approach to low energy QCD called chiral perturbation theory (ChPT) [3], there is no tree-level  $O(p^2)$  contribution to  $K^+ \rightarrow \pi^+ \gamma \gamma$  and to the neutral counterpart  $K_L^0 \rightarrow \pi^0 \gamma \gamma$ ; the leading contributions start at  $O(p^4)$  [4]. For  $K^+ \rightarrow \pi^+ \gamma \gamma$ , both the branching ratio and the  $\pi^+$  spectrum shape at  $O(p^4)$  are sensitive to one undetermined coupling-constant,  $\hat{c}$ . The next-to-leading order includes one-loop “unitarity” corrections, which are deduced from an empirical fit of the decay amplitude of  $K^+ \rightarrow \pi^+ \pi^+ \pi^-$  and contain the same constant  $\hat{c}$ , and predicts the  $\pi^+$  spectrum with a slightly different shape. The contribution of vector-meson exchange is expected to be negligible compared to the unitarity corrections [5]. The results from E787 were consistent with both the ChPT for  $\hat{c} = 1.8 \pm 0.6$  with the unitarity corrections and the ChPT for  $\hat{c} = 1.6 \pm 0.6$  at  $O(p^4)$  without the unitarity corrections; the E787 data preferred the ChPT with the corrections but were not conclusive. For  $K_L^0 \rightarrow \pi^0 \gamma \gamma$ , the amplitude at  $O(p^4)$  is determined unambiguously but the measured branching ratio,  $(1.41 \pm 0.12) \times 10^{-6}$  [6], is twice as large as the prediction; the vector meson contribution (parametrized by an effective coupling constant  $a_v$ ) is considered to be important to this decay [7].

One of the consequences of the unitarity corrections to  $K^+ \rightarrow \pi^+ \gamma \gamma$  is a nonzero amplitude at the kinematic region close to the end point  $P = 227$  MeV/ $c$  (the invariant mass of two photons  $m_{\gamma\gamma} = 0$  MeV/ $c^2$ ), as shown in Fig. 1. The partial branching ratio  $\mathcal{B}(K^+ \rightarrow \pi^+ \gamma \gamma, P > 213 \text{ MeV}/c)$  is predicted to be  $6.10_{-0.12}^{+0.16} \times 10^{-9}$  for  $\hat{c} = 1.8 \pm 0.6$  with the unitarity corrections and  $0.49_{-0.18}^{+0.23} \times 10^{-9}$  for  $\hat{c} = 1.6 \pm 0.6$  without the corrections. The former is one order of magnitude larger than the latter, and is within reach of E949. The same kinematic region in  $K_L^0 \rightarrow \pi^0 \gamma \gamma$  is known to be crucial to understand the CP-conserving component to the  $K_L^0 \rightarrow \pi^0 e^+ e^-$  decay, but experimental results on  $a_v$  [8, 9] are inconsistent and their theoretical interpretations are controversial (see [10]).

E949 is primarily designed to measure the rare decay  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  [11]. The AGS

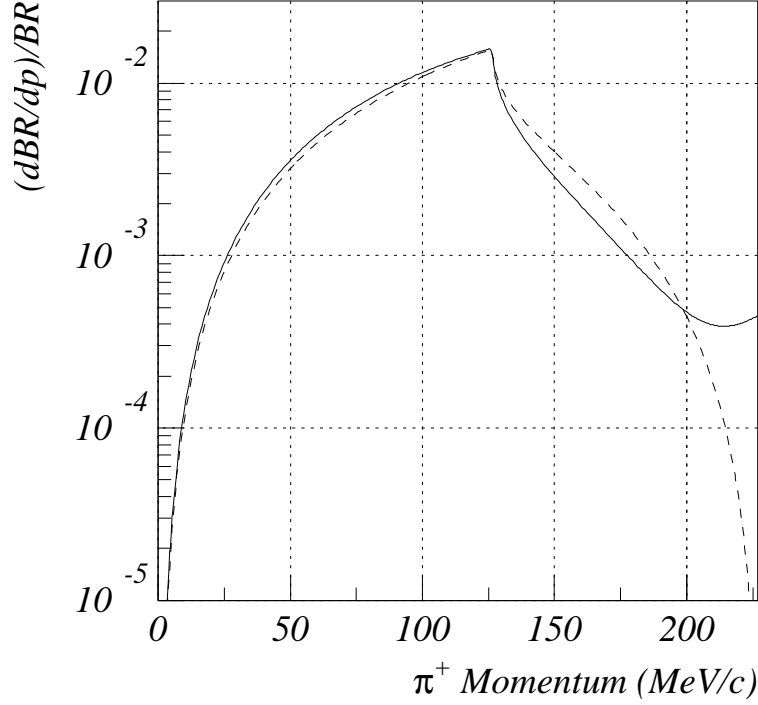


FIG. 1: Predictions for the  $\pi^+$  momentum for  $\hat{c} = 1.8$  with the unitarity corrections (solid line) and for  $\hat{c} = 1.6$  without the corrections (dashed line), respectively, in the logarithmic scale.

delivered kaons of 710 MeV/c to the experiment at a rate of  $9 \times 10^6$  per 2.2-s spill. Kaons, detected and identified by Čerenkov, tracking, and energy-loss counters, were slowed by a Be degrader, and came to rest and decayed in a scintillating-fiber target. Fig. 2 shows a diagram of the apparatus. Measurements of charged decay products were made using the target, a central drift chamber, and a cylindrical range stack (RS) composed of 17 layers of 2-cm thick plastic scintillator with two embedded layers of tracking chambers. The pion from the  $K^+ \rightarrow \pi^+ \gamma \gamma$  decay was identified by comparing the measurements of momentum, range (equivalent cm of plastic scintillator,  $R$ ), and kinetic-energy ( $E$ ), and by observation of the  $\pi^+ \rightarrow \mu^+ \rightarrow e^+$  decay sequence at rest in the RS using 500-MHz flash-ADC waveform digitizers [12]. Sets of thin trigger counters (“I” and “T” in Fig. 2) surrounding the drift chamber defined the fiducial region, and thin counters surrounding the RS suppressed the muons from  $K^+ \rightarrow \mu^+ \nu$  and  $K^+ \rightarrow \mu^+ \nu \gamma$  decays whose range is long. The trigger requirement of a sufficient time delay ( $\geq 1.5$  ns) between the Čerenkov and I counter signals ensured that the kaons had decayed at rest in the target. A hermetic calorimeter system surrounded the central region; the photons from  $K^+ \rightarrow \pi^+ \gamma \gamma$  were

detected in a lead/scintillator sandwich barrel detector (BV) surrounding the RS, while two endcap calorimeters and other detectors were used for detecting extra particles. A solenoid surrounding the BV and endcaps provided a 1 T magnetic field along the beam line.

The beam and apparatus in E949 were improved in comparison with those used in E787 [13] for the  $K^+ \rightarrow \pi^+ \gamma \gamma$  study, which was performed in 1991. The kaon beam line [14], which incorporated two stages of particle separation, reduced the pion contamination. The target, central drift chamber, and RS tracking chambers were replaced by a new target consisting of 0.5-cm square fibers, a new low-mass drift chamber [15], and straw-tube chambers, respectively. One third of the RS scintillation counters were replaced to increase the light output. A new photon detector, named barrel veto liner (BVL), was installed to added 2.3 radiation lengths of lead/scintillator sandwich material to the BV. The endcaps were replaced by new detectors consisting of undoped-CsI crystals [16], and both the target and endcaps were read out using 500-MHz CCD waveform digitizers [17]. Additional ancillary photon veto systems [18] and an LED flasher system to aid in the RS energy calibration were also introduced.

The new data were acquired in 2002, and the total exposure of kaons entering the target available for the  $K^+ \rightarrow \pi^+ \gamma \gamma$  study in E949 was  $N_K = 1.2 \times 10^{12}$ . The trigger required a kaon decay at rest, followed by a  $\pi^+$  track which came to rest in the RS and coincident activity due to electromagnetic shower in both the BVL and BV, and no extra particles in the endcap or RS counters. The RS counter where the  $\pi^+$  track came to rest, called the “stopping counter”, was requested to be in the 15th or 16th layer in order to suppress the  $\pi^+$  tracks from the  $K^+ \rightarrow \pi^+ \pi^0$  decay ( $K_{\pi 2}$ ) with  $P = 205$  MeV/ $c$ ,  $R = 30.4$  cm, and  $E = 108$  MeV. An improved trigger system [19] of E949, including a programmable trigger board, allowed more efficient running and reduced deadtimes. A total of  $1.1 \times 10^7$  events met the trigger requirements.

The signature of  $K^+ \rightarrow \pi^+ \gamma \gamma$  was a kaon decay at rest with a  $\pi^+$  track in the RS in the kinematic region above the  $K_{\pi 2}$  monochromatic peak and photons reconstructed in the BVL and BV calorimeters. The accepted region of  $\pi^+$  was  $213 \text{ MeV}/c < P < 234 \text{ MeV}/c$ ,  $33.5 \text{ cm} < R < 41.3 \text{ cm}$ , and  $116 \text{ MeV} < E < 135 \text{ MeV}$ ; the lower limits corresponded to 3.3, 2.3, and 2.6 standard-deviations above the  $K_{\pi 2}$  peak, respectively, in the E949 apparatus. Due to the improvements in the kinematic reconstruction, the region was enlarged from  $P > 215 \text{ MeV}/c$  in E787 [2] and a constrained kinematic fit for consistency with  $K^+ \rightarrow \pi^+ \gamma \gamma$

was not needed in the offline analysis. The timing and energy ( $E_\gamma$ ) of the photons were determined by grouping adjacent hit modules in BV and BVL to identify isolated photon showers (“clusters”). The hit position in each module along the beam axis ( $z$ ) was calculated from the end-to-end time and energy differences; the azimuthal angle ( $\phi$ ) of the hit position was determined up to the segmentation of the modules. The location of the photon shower in  $z$  and  $\phi$  was obtained by an energy-weighted average of the hit positions and was used, in conjunction with the kaon-decay vertex position in the target, to determine the polar and azimuthal angles of the photon to the  $\pi^+$  track ( $\theta_{\pi+\gamma}$  and  $\phi_{\pi+\gamma}$ ). Since the opening angle between two photons from  $K^+ \rightarrow \pi^+\gamma\gamma$  gets narrower for the events whose  $\pi^+$  momentum is close the kinematic end point, the two photons of about one half of the signal events form a single cluster in BVL and BV within their limited position-resolutions; the events with exactly one or two clusters were therefore accepted in the offline analysis. The highest-energy cluster should satisfy  $50 \text{ MeV} < E_\gamma < 320 \text{ MeV}$ ,  $\theta_{\pi+\gamma} > 155^\circ$ , and  $\phi_{\pi+\gamma} > 155^\circ$ . The energy of the lower-energy cluster, if exists, should be at least 10 MeV.

Background sources from kaon decays at rest are: the  $K_{\pi 2}$  decay due to mismeasurements of the  $\pi^+$  and the two photons (“mismeasured”), including detection inefficiency of the softer of the photons from  $\pi^0$  if exactly one cluster is reconstructed; the  $K_{\pi 2}$  decay due to the disappearance of the softer photon through overlap with the  $\pi^+$  track in the RS (“overlap”); and the kaon decays with a muon, misidentified as  $\pi^+$ , and some photons in the final state, such as  $K^+ \rightarrow \mu^+\nu\gamma$  and  $K^+ \rightarrow \pi^0\mu^+\nu$  decays, as well as the  $K_{\pi 2}$  decay whose  $\pi^+$  decays in flight to  $\mu^+$  in the detector (“mudecay”). The  $K_{\pi 2}$  decay in flight in the beam line before the kaon comes to rest (“DIF”), if the  $\pi^+$  momentum is Lorentz-boosted and satisfies the conditions for  $K^+ \rightarrow \pi^+\gamma\gamma$ , is the background source from the incident beam particles; other beam-related backgrounds (e.g. multiple beam particles into the detector) were found to negligible. These backgrounds were studied from the data by establishing two independent sets of offline selection criteria (“cuts”) for each. For the background sources from kaon decays at rest, one set consisted of the cuts on the accepted region of the  $\pi^+$  momentum, range and kinetic energy. The other set consisted of: the cuts on the invariant mass of two photons (to reject events with  $m_{\gamma\gamma} > 100 \text{ MeV}/c^2$ ), on extra activity (to reject events with activity not associated with the  $\pi^+$  and the candidate signal photons [20]), and on the photon clusters (to reject events with two photons from a  $\pi^0$  which hit the same or adjacent modules in BVL and BV and form a single cluster [21, 22]) to the mismeasured

background; the cuts on the overlapping photon in the RS (to reject events with a RS counter in which the measured energy was larger than expected from the reconstructed range in that counter [22]) to the overlap background; and the cuts on the  $\pi^+ \rightarrow \mu^+ \rightarrow e^+$  decay sequence, recorded in the RS stopping counter, to the mudecay background, respectively. The DIF background was studied by the cuts on the delay ( $\geq 2$  ns) between the  $\pi^+$  time and the  $K^+$  time measured in the target and the cuts on the difference between the  $\pi^+$  time in the RS and the  $K^+$  time in the Čerenkov counter.

In these studies, we inverted at least one of these cuts on the events in order to enhance the background collected by the trigger as well as to prevent candidate events from being examined before the background studies were completed. Possibilities of a correlation between two sets of cuts and of a biased estimate of the effectiveness of the cuts, the level of signal acceptance as a function of cut severity, the check of the observed background levels near but outside the signal region in comparison with the predicted background rate, etc. were studied [23] by following the procedures developed through the  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$  analysis in E949 and E787 [11, 24]. The background levels anticipated with the final analysis cuts were  $b_{mismeasured} = 0.017 \pm 0.006$ ,  $b_{overlap} = 0.065 \pm 0.065$ ,  $b_{mudecay} = 0.090 \pm 0.020$ ,  $b_{DIF} = 0.025 \pm 0.014$ . In total,  $b = 0.197 \pm 0.070$  background events were expected in the signal region.

The acceptance ( $A$ ) and the single event sensitivity ( $SES$ ) for  $K^+ \rightarrow \pi^+ \gamma \gamma$ :  $A = (2.99 \pm 0.07) \times 10^{-4}$  and  $SES = 3.72 \times 10^{-9}$  for  $\hat{c} = 1.8$  with the unitarity corrections and  $A = (1.18 \pm 0.04) \times 10^{-4}$  and  $SES = 9.40 \times 10^{-9}$  for  $\hat{c} = 1.6$  without the corrections, were derived from the acceptance factors in Table I, the total kaon exposure  $N_K = 1.2 \times 10^{12}$ , and the  $K^+$  stop efficiency, which is the fraction of kaons entering the target that came to rest and was measured with the  $K_{\pi 2}$  events collected by the same trigger, of  $0.754 \pm 0.024$ . The former sensitivity was below the predicted branching ratio of  $6.10 \times 10^{-9}$ . In order to verify that the sensitivity estimations were correct, the sample of  $K^+ \rightarrow \mu^+ \nu$  decays accumulated by a calibration trigger was analyzed and the measured branching ratio,  $0.628 \pm 0.020$ , was consistent with the value in [6]; this indicates that the systematic uncertainty in this study is small.

After imposing all analysis cuts, no events were observed in the signal region (Fig. 3). The group of 74 events around  $R = 32$  cm and  $E = 110$  MeV [25] was due to the  $K_{\pi 2}$  background. Taking 2.24 events instead of zero according to the unified approach [6, 26] with the back-

ground contribution of 0.197 events, we set a 90% confidence level (C.L.) upper limit on the  $K^+ \rightarrow \pi^+ \gamma \gamma$  branching ratio  $8.3 \times 10^{-9}$  for  $\hat{c} = 1.8$  with the unitarity corrections and  $2.1 \times 10^{-8}$  for  $\hat{c} = 1.6$  without the corrections. The systematic uncertainty was not taken into consideration in deriving the limits. For the purpose of comparison with the previous E787 results, a 90% C.L. upper limit for the total  $K^+ \rightarrow \pi^+ \gamma \gamma$  branching ratio assuming the phase-space kinematic distribution was calculated; the limit  $6.0 \times 10^{-8}$  is 8.3 times better than the same limit in E787 [2].

The data described above were used to set a 90% C.L. upper limit on the branching ratio for the  $K^+ \rightarrow \pi^+ \gamma$  decay, which is forbidden by angular-momentum conservation and by gauge invariance but is allowed in non-commutative standard models [27]. The previous limit from the E787 study performed in 1996 and 1997 was  $3.6 \times 10^{-7}$  [22], and the new limit is  $2.3 \times 10^{-9}$ . The data also set limits on sequential decays in the form  $K^+ \rightarrow \pi^+ X^0$ ,  $X^0 \rightarrow \gamma \gamma$ , where  $X^0$  is any short-lived neutral particle with a mass  $m_{X^0}$  smaller than 100 MeV/ $c$  decaying into two photons. Fig. 4 shows the limit as a function of  $m_{X^0}$  for different lifetimes.

The results from this study cannot confirm nor rule out the ChPT including the unitarity corrections, but the obtained upper limits are the tightest ones that have been experimentally achieved on  $K^+ \rightarrow \pi^+ \gamma \gamma$ ,  $K^+ \rightarrow \pi^+ \gamma$ , and  $K^+ \rightarrow \pi^+ X^0$  decays. The analysis, which was limited by the total exposure of kaons available at the data taking in 2002, has proved that the experiment with kaon decays at rest is suitable to study  $K^+ \rightarrow \pi^+ \gamma \gamma$  in the  $\pi^+$  momentum region close to the end point. The possibility to observe signal events of  $K^+ \rightarrow \pi^+ \gamma \gamma$  in the kinematic region, if the ChPT including the unitarity corrections is correct, gives further impetus for additional measurements.

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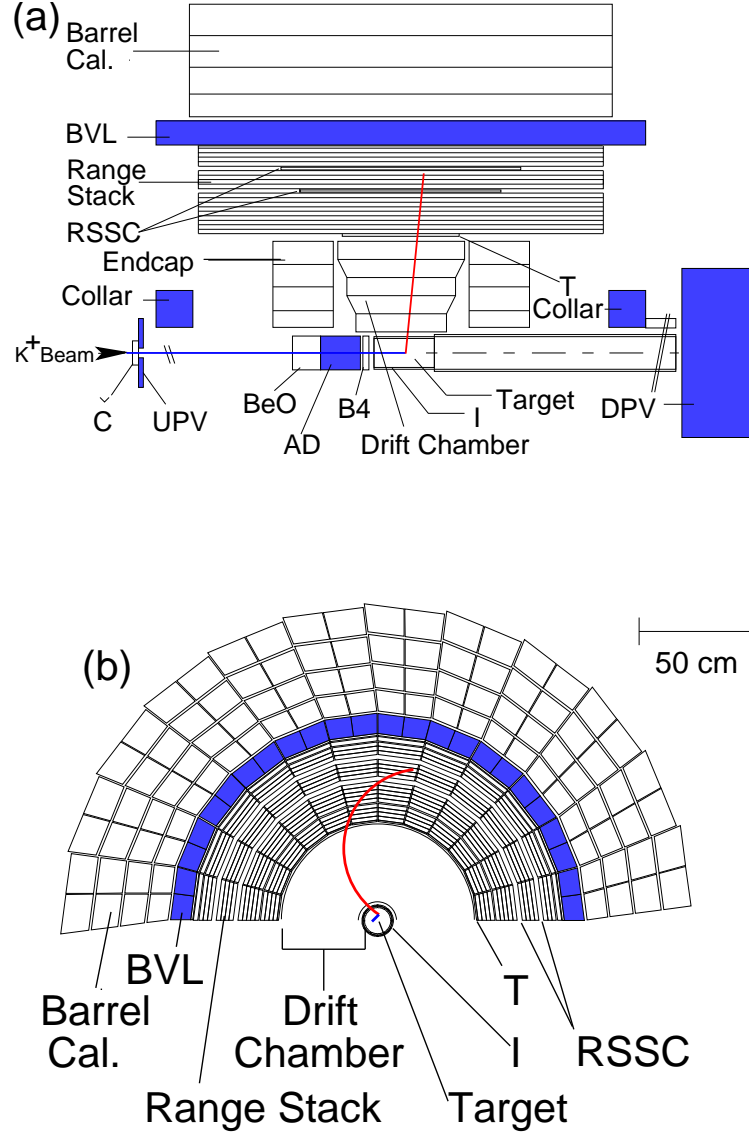


FIG. 2: Schematic side (a) and end (b) views of the upper half of the E949 detector. Č: Čerenkov counter; B4: energy-loss counters; I and T: inner and outer trigger scintillation counters; RSSC: RS straw-tube tracking chambers. New or upgraded subsystems for E949 (shaded) included the barrel veto liner (BVL), collar, upstream photon veto (UPV), active degrader (AD), and downstream photon veto (DPV). In addition, the outer trigger detectors and other trigger and electronics systems were improved in E949.

Acceptance factors	UC	w/o UC	samples
Trigger (in $10^{-1}$ )	0.346	0.061	MC
$\pi^+$ reconstruction cuts	0.996	0.996	$K_{\mu 2}$
$\pi^+$ fiducial cuts	0.898	0.626	MC
$\pi^+$ stop without nuclear interaction or decay-in-flight	0.492	0.578	MC
Waveform digitizer ( $\pi^+ \rightarrow \mu^+ \nu$ ) cuts	0.349	0.349	$\pi_{scat}$
$\gamma$ reconstruction and fiducial cuts	0.530	0.492	MC, $K_{\pi 2}$ ,
Extra photon veto cuts	0.216	0.173	MC, $K_{\pi 2}$ ,
$\pi^+$ kinematic cuts	0.537	0.537	$K_{\pi 2}$ , $\pi_{scat}$
Other cuts on beam and target	0.507	0.507	$K_{\mu 2}$
Trigger-counter efficiency	0.936	0.936	$K_B$
correction factor	1.93	7.15	MC
Total acceptance (in $10^{-4}$ )	2.99	1.18	

TABLE I: Acceptance factors for the  $K^+ \rightarrow \pi^+ \gamma \gamma$  decay, for  $\hat{c} = 1.8$  with the unitarity corrections (“UC”) and for  $\hat{c} = 1.6$  without the corrections (“w/o UC”), and the samples used to determine them. “ $K_{\pi 2}$ ”, “ $K_{\mu 2}$ ”, “ $\pi_{scat}$ ”, and “ $K_B$ ” mean the data samples of  $K_{\pi 2}$  decays,  $K^+ \rightarrow \mu^+ \nu$  decays, scattered beam pions, and kaons entering the target, respectively, which were accumulated by calibration triggers simultaneous to the collection of signal candidates. “MC” means the sample generated by Monte Carlo simulation; the simulation generated the  $K^+ \rightarrow \pi^+ \gamma \gamma$  decay in  $P > 200$  MeV/ $c$ , and the correction factor in this table was multiplied to convert the acceptance for the partial branching ratio in  $P > 200$  MeV/ $c$  to be in  $P > 213$  MeV/ $c$ , by assuming the  $\pi^+$  spectrum shape in each case.

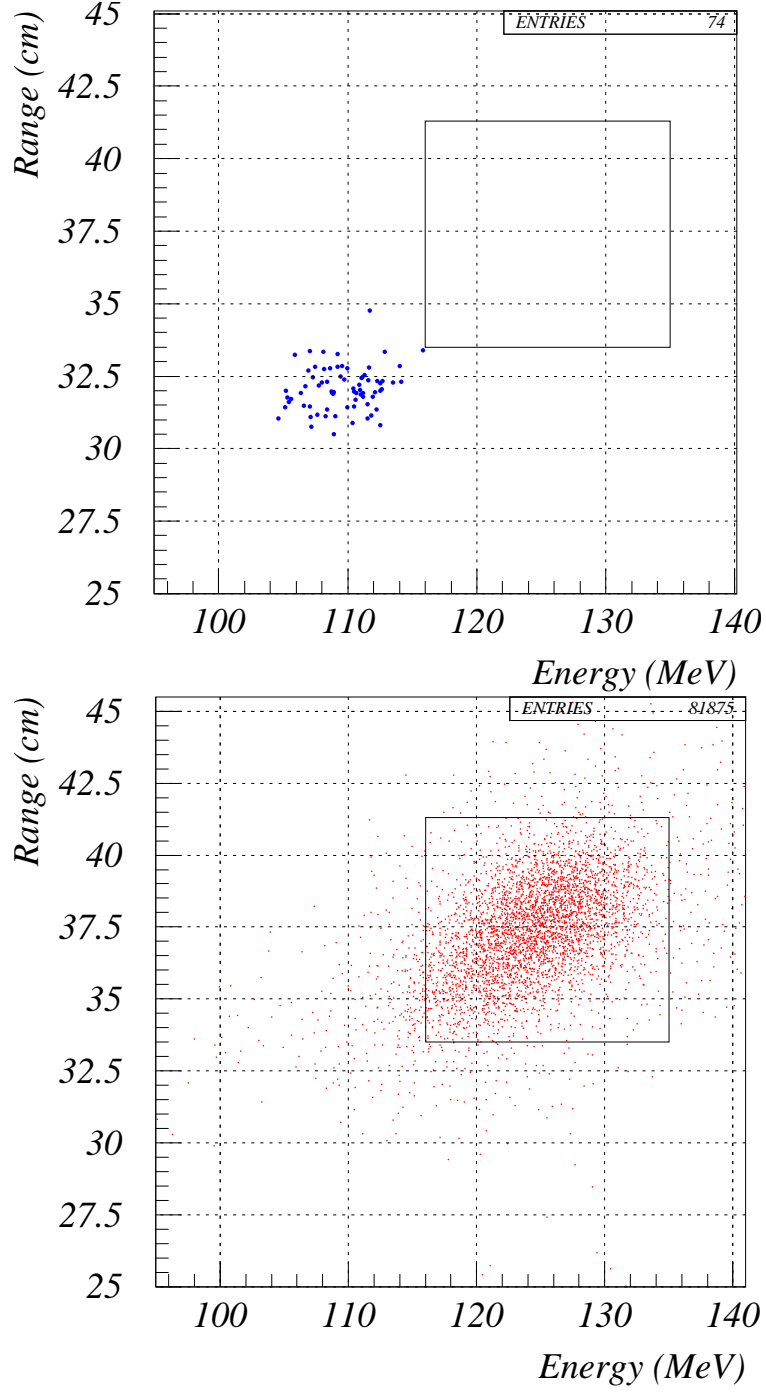


FIG. 3: (a) Range vs. kinetic energy plot of the events with all analysis imposed. The box indicates the signal region for  $K^+ \rightarrow \pi^+ \gamma \gamma$ . (b) The simulated distribution of events from  $K^+ \rightarrow \pi^+ \gamma \gamma$  decay.

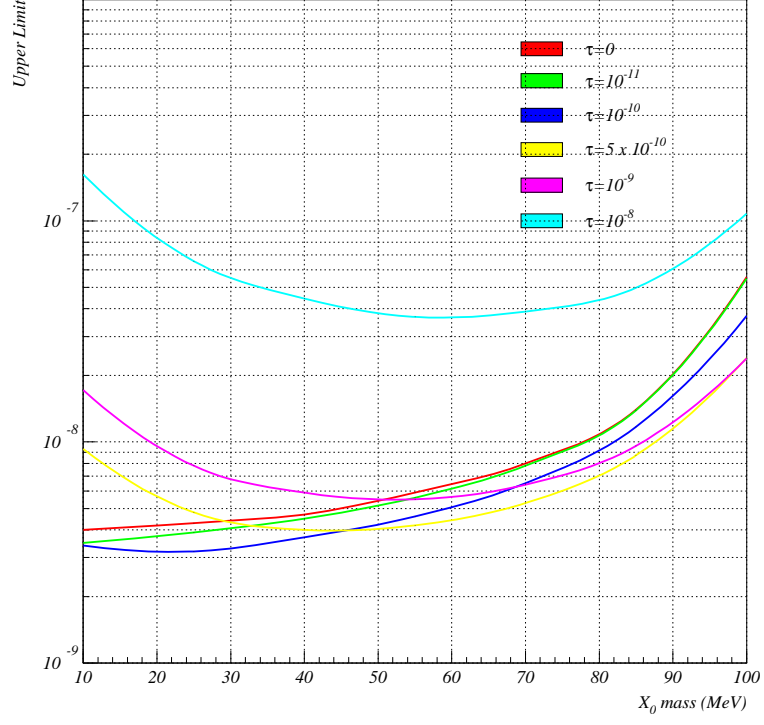


FIG. 4: The 90% C.L. upper limits for the branching ratio of  $K^+ \rightarrow \pi^+ X^0$ ,  $X^0 \rightarrow \gamma\gamma$  for different  $X^0$  lifetimes ( $\tau$ ) in seconds as a function of  $X^0$  mass.

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